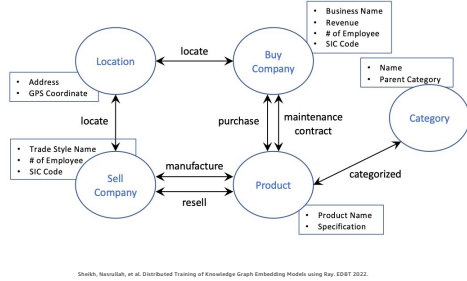




Motivating Example

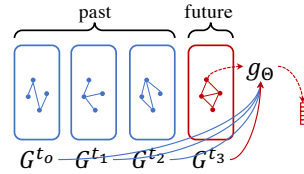


Sheikh, Nasrullah, et al. Distributed Training of Knowledge Graph Embedding Models using Ray. EDOT 2022.

Discrete Time Dynamic Graphs (DTDGs)

Discrete-time Dynamic Graphs (DTDGs)

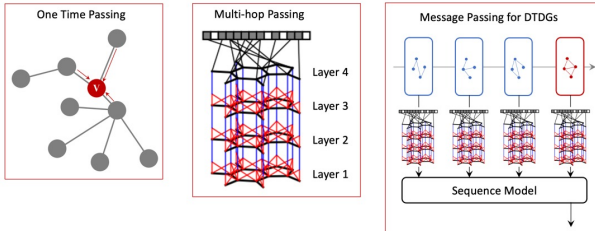
- $G^t = (G^{t_0}, \dots, G^{t_n})$ # a sequence of static graphs (snapshots)
- $G^t = \{V^t, E^t, X^t\}$ # vertex, edge and feature sets
- $V^t = \{v_1, \dots, v_{|V^t|}\}$ # a set of nodes
- $E^t = \{e_1, \dots, e_{|E^t|}\}$ # a set of edges
- $X^t = \{x_1, \dots, x_{|V^t|}\}$ # a set of node features



Problem

Learn the future node representation
-- predicting the future based on the past.

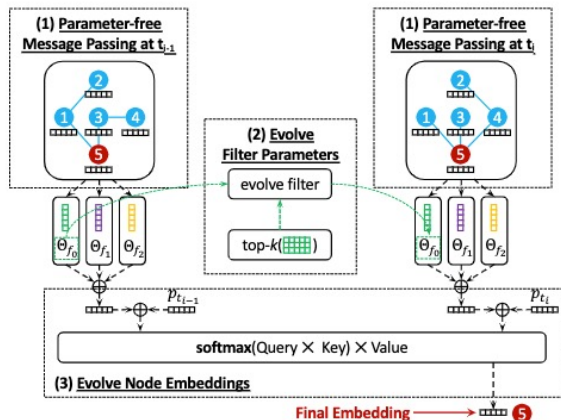
Existing Message Passing-based Solutions



Question 1. How can the model be efficiently trained on large-scale DTDGs to exploit hardware accelerators with small memory footprint?

Question 2. How can the model effectively capture the changing dynamics of the graphs?

Our Approach – Scalable Evolving Inception Graph Neural Network (SEIGN)



Parameter-free Message Passing

$$Z^{t_i} = \xi \left(\sigma \left(\bigoplus_{j=0}^k \mathcal{A}_j^{t_i} \chi^{t_i} \theta_{f_j}^{t_i} \right) \theta_o \right)$$

$\mathcal{A}_j^{t_i}$ is a linear diffusion operator.

$\mathcal{A}_j^{t_i} \chi^{t_i}$ computes the node aggregated messages for j^{th} hop. The computation does not involve learnable parameters. Therefore, such a message passing can be done in a preprocessing step.

Benefit: 1) less node dependencies 2) less parameters to train

The embeddings Z^{t_i} for a snapshot are generated based on a set of graph diffusion operations covering multiple neighborhood sizes, analogous to the popular Inception network.

Benefit: better embedding expressivity

Evolving Parameters over Time

$\Theta_{f_j}^{t_i}$ is a learnable matrix that transforms the node aggregated messages for j^{th} hop. Sharing these parameters across time results in poor performance. We propose to use a sequence model to regulate them over time.

Benefit: better embedding expressivity

Evolving Node Embedding over Time

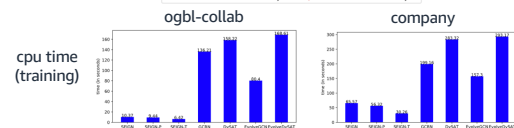
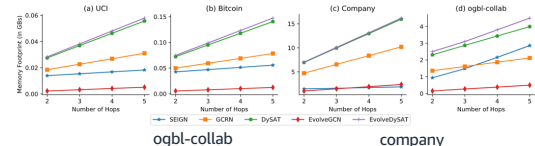
$Z_v = \{z_v^{t_0} + p_{t_0}, \dots, z_v^{t_{|T|}} + p_{t_{|T|}}\}$ is the concatenated node and positional embeddings for node v over time. We propose to use the self-attention model to generate the final embedding for v from its embeddings over time.

Benefit: better embedding expressivity

Experimental Evaluation

Methods	UCI			Bitcoin			Company			ogbl-collab		
	AUC \uparrow	AP \uparrow	F1 \uparrow (0.5)	AUC \uparrow	AP \uparrow	F1 \uparrow (0.5)	AUC \uparrow	AP \uparrow	F1 \uparrow (0.5)	AUC \uparrow	AP \uparrow	F1 \uparrow (0.5)
GCN	74.35 \pm 1.8	74.96 \pm 1.2	68.90 \pm 0.9	83.58 \pm 1.2	84.68 \pm 1.1	77.86 \pm 0.8	88.75 \pm 0.3	85.15 \pm 0.4	82.14 \pm 0.3	93.45 \pm 0.1	93.29 \pm 0.0	87.98 \pm 0.1
GAT	68.62 \pm 3.2	67.75 \pm 3.0	61.93 \pm 2.8	84.25 \pm 0.6	83.62 \pm 0.6	79.80 \pm 0.4	84.10 \pm 1.2	81.84 \pm 0.9	77.82 \pm 1.0	92.79 \pm 0.3	92.58 \pm 0.3	88.59 \pm 0.2
SEIGN	74.98 \pm 0.3	69.92 \pm 0.4	74.54 \pm 0.2	87.03 \pm 0.1	85.70 \pm 0.1	84.89 \pm 0.2	92.72 \pm 0.1	89.11 \pm 0.1	86.22 \pm 0.2	97.07 \pm 0.0	96.10 \pm 0.1	82.80 \pm 0.1
GCRN	77.21 \pm 0.7	75.28 \pm 0.8	74.19 \pm 0.7	87.81 \pm 0.2	88.02 \pm 0.2	80.21 \pm 0.2	91.65 \pm 0.2	87.05 \pm 0.2	84.71 \pm 0.2	96.47 \pm 0.0	96.18 \pm 0.1	84.54 \pm 0.2
DySAT	77.46 \pm 0.6	76.54 \pm 0.6	73.06 \pm 0.7	88.82 \pm 0.1	88.19 \pm 0.2	82.01 \pm 0.2	92.45 \pm 0.0	88.07 \pm 0.1	86.10 \pm 0.0	95.18 \pm 0.2	95.05 \pm 0.3	87.34 \pm 0.1
EvolveGCN	76.09 \pm 1.0	75.65 \pm 0.9	71.07 \pm 0.9	85.53 \pm 0.4	84.82 \pm 0.5	79.23 \pm 0.3	89.22 \pm 0.1	86.40 \pm 0.2	79.84 \pm 0.1	96.06 \pm 0.2	95.61 \pm 0.2	91.01 \pm 0.3
EvolveDySAT	80.49 \pm 0.6	78.08 \pm 0.7	74.02 \pm 0.4	89.38 \pm 0.1	90.12 \pm 0.0	76.32 \pm 0.1	92.78 \pm 0.0	88.78 \pm 0.0	86.25 \pm 0.1	96.09 \pm 0.0	96.13 \pm 0.1	87.40 \pm 0.0
SEIGN-P	79.82 \pm 0.5	78.55 \pm 0.4	75.44 \pm 0.4	88.44 \pm 0.1	87.04 \pm 0.1	83.61 \pm 0.2	93.35 \pm 0.1	89.25 \pm 0.0	87.35 \pm 0.0	97.50 \pm 0.1	97.34 \pm 0.1	86.78 \pm 0.2
SEIGN-T	76.86 \pm 0.3	72.49 \pm 0.2	73.08 \pm 0.2	88.51 \pm 0.2	86.56 \pm 0.2	84.41 \pm 0.1	93.26 \pm 0.2	88.28 \pm 0.2	86.86 \pm 0.1	97.35 \pm 0.1	96.62 \pm 0.1	82.20 \pm 0.2
SEIGN	80.83 \pm 0.3	81.36 \pm 0.2	71.81 \pm 0.2	90.12 \pm 0.0	91.13 \pm 0.1	81.89 \pm 0.1	94.34 \pm 0.1	90.09 \pm 0.1	88.39 \pm 0.1	98.33 \pm 0.1	98.49 \pm 0.0	86.85 \pm 0.1

memory footprint (pytorch backward() call)



Conclusion

- We introduce a simple and efficient representation learning method for DTDGs.
- We propose to simultaneously evolve the graph model parameters and the representations from each graph snapshot to effectively capture the changing dynamics of the DTDGs.
- We further introduce an evolving graph inception architecture in SEIGN for DTDGs which enables efficient graph mini-batch construction and incurs a considerably lower training memory footprint.
- We evaluate the effectiveness of SEIGN in a position study and an ablation study. The position study compares our method against state-of-the-art approaches for an unsupervised training task on publicly available benchmarks as well as a real industrial dataset. We also demonstrate the efficiency of training SEIGN by providing various compute and memory profiles.